

- ❑ A brief discussion of aerodynamics is needed in order to appreciate the complexity of weapon system design
  - We're not planning to build a missile, but...
  - We need to understand basic aerodynamic principles in order to design a weapon system
- ❑ The aerodynamic building blocks to be discussed include
  - Basic aerodynamic principles (forces and moments)
  - Missile body type characteristics
  - Projectile stability
- ❑ These building blocks will be referenced in other lectures as we discuss numerous topics
  - Guidance law development
  - Weapon system design
  - Track processing (track filtering)
- ❑ First, some basic terms used in aerodynamics must be discussed

Gregg Bock

## Missile Aerodynamics

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## Mach

Important Terms in Missile Engineering

- ❑ Speed can be measured using the speed of sound as a base scale
- ❑ This measurement of speed is referred to as Mach (M)
 
$$M = \frac{V_{\text{Missile}}}{V_{\text{Sound}}}$$
- ❑ Mach number represents the ratio of ordered energy to random energy
- ❑ All aerodynamic coefficients are affected by the Mach number.
  - Variations with Mach number become more apparent as  $M > 1$
- ❑ Sound travels at 1116 ft/sec at sea level
  - The speed of sound varies as a function of ambient temperature
 
$$V_{\text{Sound}} \cong 49 \sqrt{T_{\text{amb}}}$$

\*  $T_{\text{amb}}$  is temperature in Rankine (518.7° at sea level)

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## What – a – sonic?

Important Terms in Missile Engineering

- ❑ Streamlines define how air flows past the body as the body cuts through the atmosphere
- ❑ Streamlines differ as the speed in which air flows past the body increases
- ❑ Four regions of missile speed
  - Subsonic (Mach < 1.0)
  - Transonic (Mach ~ 1.0)
  - Supersonic (1.0 < Mach < 5.0)
  - Hypersonic (Mach > 5.0)
- ❑ Air flow patterns over specific geometric shapes (correlating to specific missile parts) are dependent upon the regions listed above

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## Dynamic Pressure (Q)

Important Terms in Missile Engineering

- ❑ Q is defined as
 
$$Q = \frac{\rho}{2} V^2 \cong (0.7)(P) M^2$$

↔ This is the more common definition when  $M > 0.5$
- ❑ Where
  - $\rho$  is the ambient density (slugs/ft<sup>3</sup>) (kg/m<sup>3</sup>)
  - $V$  is the missile velocity (ft/sec) (m/sec)
  - $P$  is the ambient pressure (lbs/ft<sup>2</sup>) (Pa = N/m<sup>2</sup>)
  - $M$  is the Mach number
- ❑ 0.7 is approximately one half the specific heat ratio of air
- ❑ Q is a function of both speed and altitude

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The Ability of the Missile to Maneuver is Directly Related to the Dynamic Pressure of the Missile

## Pressure Waves

Important Terms in Missile Engineering

- ❑ Pressure waves are the result of molecules of air being pushed together due to a body forcing its way through the atmosphere
- ❑ Pressure waves travel at the speed of sound (Mach 1)
- ❑ They travel in all directions from the disturbance
  - Similar to waves in a pool after throwing a rock in the water
  - As the speed of the flying body increases, the shape of the pressure circles change

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The Next Slide Illustrates Pressure Waves for Various Missile Speeds



Figure 6: Lockhead Martin  
Pressure waves for a very slow moving body

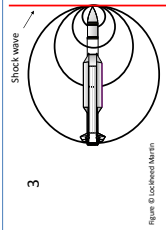


Figure 6: Lockhead Martin

A shock wave is created where the air flow past the body is equal to the speed of the pressure wave (Mach 1)

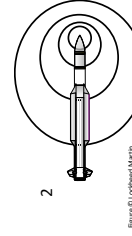


Figure 6: Lockhead Martin  
Pressure waves for a body travelling at subsonic speeds

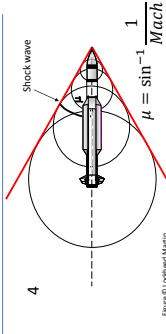


Figure 6: Lockhead Martin

The angle,  $\mu$ , at which a supersonic shockwave is formed can be calculated

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- Angle of attack ( $\alpha$ ) is the angle between the missile body center line ( $M_{CL}$ ) and the velocity vector of the missile.
  - Also referred to as the angle between the missile body axis and the wind axis.
- Angle of attack
  - Increases drag on the missile (more missile body is exposed)
  - Angle of attack is required for a missile to change direction

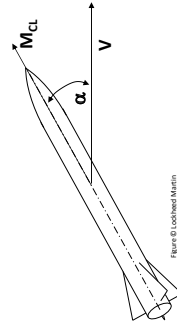


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There is a Great Picture on the Next Page to Illustrate This...

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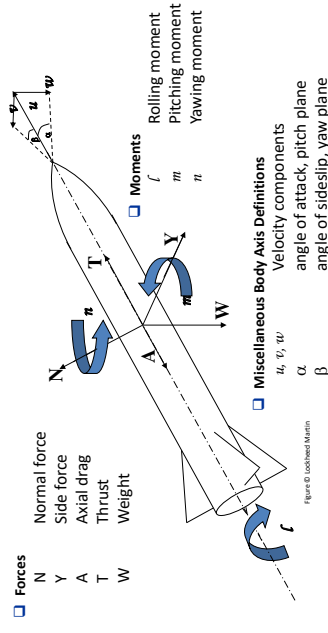


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- The missile seeker is often found within the nose cone of the missile and is the device used to detect the missile's intended target
- The radome is the comprised of extremely hard material that allows either IR or RF waves to pass from the environment to the missile seeker
  - The shape of the radome greatly influences the missile's aerodynamic performance as well as its ability to track a target effectively
- The most common seeker types are described below

| Seeker Type   | Description                                                                                                                                                 |
|---------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Active        | Radar located in the nose of the missile that transmits and receives RF signals                                                                             |
| Semi-Active   | Receiver located in the nose of the missile that receives RF signals reflected off the target which had originated from a source not located on the missile |
| Passive       | Receiver receives signals emanating from the target but the source of the signal was not provided by the combat system                                      |
| Infrared (IR) | Tracks the target using infrared (heat) imaging                                                                                                             |

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- Forces and Moments are defined in a body axis reference system
  - N – normal force (force perpendicular to the body axis)
  - Y – side force (force perpendicular to the body axis)
  - A – axial force (force along body axis, thrust and drag)
  - m – pitching moment about the lateral axis
  - n – yawing moment about the normal axis
  - l – rolling moment about the center line axis

- Force coefficients:
 
$$C_N = \frac{N}{Q S_{Ref}} \quad C_Y = \frac{Y}{Q S_{Ref}} \quad C_A = \frac{A}{Q S_{Ref}}$$
- Where:
  - $S_{Ref}$  is the reference area
- For missiles,  $S_{Ref}$  is usually considered to be the maximum cross-sectional area
  - Compute the reference area using the diameter of the missile (cross sectional area)
- For airplanes,  $S_{Ref}$  is defined by the area of the wing

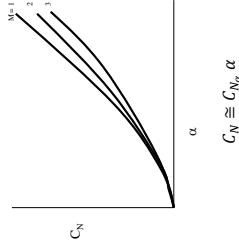
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- Moment coefficients:
 
$$C_m = \frac{m}{Q S_{Ref} L_{Ref}} \quad C_n = \frac{n}{Q S_{Ref} L_{Ref}} \quad C_l = \frac{l}{Q S_{Ref} L_{Ref}}$$
- $S_{Ref}$  is the reference area (max. body cross sectional area)
- $L_{Ref}$ 
  - For missiles,  $L_{Ref}$  is a reference length, or body diameter (more on this later)
  - For airplanes,  $L_{Ref}$  is related to the wing chord
- Moment coefficients are taken about a referenced center of gravity
  - Center of gravity changes as fuel/propellant is burned off
  - i.e. the interceptor rotates about its center of gravity due to a non-zero moment

- $C_x$  and  $C_m$  are proportional to the angle of attack ( $\alpha$ )
  - Influenced by  $\beta$
- $C_y$  and  $C_z$  are proportional to the side-slip angle ( $\beta$ )
  - Influenced by  $\alpha$
- $C_x$  is independent of both  $\alpha$  and  $\beta$ .
- $C_z$  is dependent upon both  $\alpha$  and  $\beta$

- A typical  $C_x$  vs.  $\alpha$  plot at various Mach numbers would look like this:
- This allows us to write the following:



- For each Mach number,  $C_N$  as a function of  $\alpha$  is nearly linear for small  $\alpha$
- This means that each  $C_N$  is linear as a function of Mach
- One can see that to get a good first order approximation, one could assume an average Mach resulting in

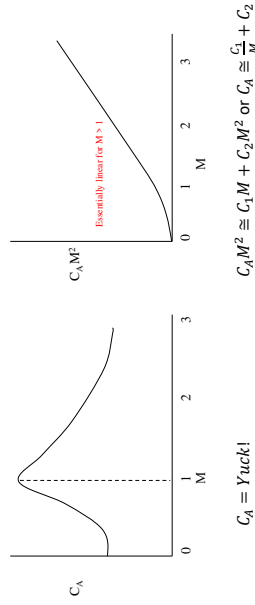
$$C_{N\alpha} = \left( \frac{\partial C_N}{\partial \alpha} \right)_M$$

**$C_{N\alpha}$  is Considered a Constant!**

- Coefficients vary as a function of
  - Mach (M)
  - Angle of attack ( $\alpha$ )
  - Sideslip ( $\beta$ )
  - Roll ( $\phi$ )
- Coefficients are determined by theoretical design as well as wind tunnel test analysis
- Coefficients are referred to as proportionality factors
- Scalability
  - Makes wind tunnel work with models very effective
  - Aerodynamic forces scale by  $L^2$  for similar configurations
  - Aerodynamic moments scale by  $L^3$  for similar configurations

- Axial drag ( $A$ ) is far more sensitive to Mach than the normal force (N) or side force (Y)
- Normal force is nearly independent of Mach
  - Provided the wings are slender and pointed
  - Low aspect ratio (delta shape)
- Coefficients associated with the missile's rotational rates
  - Very complex
  - Burdensome to compute
  - They are not covered in this discussion

- A typical  $C_x$  vs. Mach plot would look like this:
- Since  $C_x$  is not very easy to describe as a function of M, we often express it in this manner



- The induced drag ( $C_{Di}$ ) is the component of lift that resists missile motion
- It is the penalty one must pay to generate lift force on the missile
- The maneuvering efficiency (per G) is a function of induced drag

$$C_{Di} = C_N \alpha = (C_N)^2 \alpha^2$$

- One can represent maneuver G's as

$$n_y = \frac{N}{W} = (C_N)^2 \frac{Q S_{ref}}{W}$$

- Therefore

$$\frac{n_y}{\alpha} = (C_N)^2 \frac{Q S_{ref}}{W}$$

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- Normal and axial forces translate into lift and drag forces
  - Lift force is perpendicular to the velocity vector
  - Drag force is along the velocity vector
- Sometimes it is desired to have the forces defined by the orientation of the missile velocity vector rather than the missile center line
- *There is no lift without drag*
  - It is a basic property of aerodynamics

It is Desirable to Have a High Lift-To-Drag Ratio

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- Lift and drag forces describe the forces acting on the missile in a plane defined by the missile velocity vector and the directions orthogonal to it
- The Normal and Axial forces can be defined as Lift and Drag terms as follows:
  - $L = N \cos(\alpha) - A \sin(\alpha)$
  - $D = A \cos(\alpha) + N \sin(\alpha)$
- We can simplify this to
  - $L \cong N$
  - $D \cong A + N \alpha$
- Lift and Drag can be normalized in the same manner as the Normal and Axial forces
  - $C_L \cong C_N$
  - $C_D \cong C_A + C_N \alpha$

Zero-Lift Drag,  $C_{D0}$

Induced drag,  $C_{Di}$

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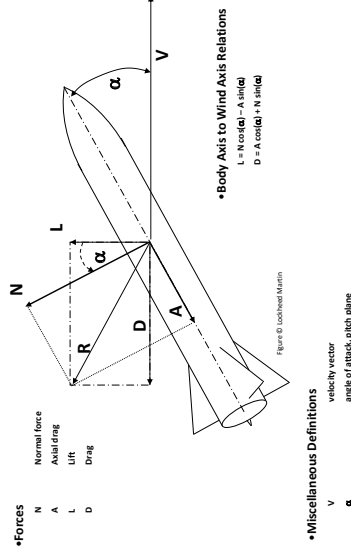
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- Induced drag is the penalty paid for a change of direction by the missile
  - It can be expressed as a function of the square of the acceleration.
- $$C_{Di} = \frac{n_y^2 W^2}{(C_N)^2 Q^2 S_{ref}^2}$$
- Note which factors contribute to high induced drag, and which contribute to low induced drag
  - The objective of a guidance law is for the missile to hit the target with the greatest amount of kinetic energy (velocity) possible
    - When developing a guidance law, the goal is to minimize the integral of the commanded acceleration over the time of flight as it should also reduce the induced drag
    - i.e.

$$I = \int_0^T n_y^2 dt$$

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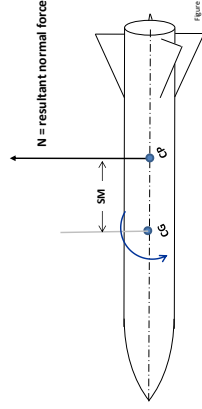
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- The missile must be designed for stability during flight
  - Forces and moments acting upon the interceptor can easily result in an unstable flying configuration
  - One of the key concepts in understanding stable flight is static margin
- Static Margin is defined as the distance the center of gravity is aft of the center of pressure
  - $SM = CG - CP$
  - The interceptor is unstable when  $SM > 0$
  - CG must be forward of CP
  - Rule of thumb:  $SM \cong -0.50 d$  (50% of the missile diameter)
- Center of Pressure is the centroid of the longitudinal normal force distribution
  - Shifts due as a function of Mach and angle of attack
  - Shift can be minimized using long slender wings
- Center of Gravity is the centroid of the gravitational forces acting on a body
  - Shifts as a function of propellant burn off

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- In a stable configuration ( $SM < 0$ ), the static margin is directly related to a resultant moment about CG
  - $m = N (SM)$
- Controlling that resultant moment is critical to ensure stability is maintained
  - It does not have to be zero, just controlled



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## Rowan University Deriving the Trim Condition

- Define the moments due to forces N and  $\Delta N_t$

$$m = N (SM) = \left( \frac{C_N}{\alpha} \right) \alpha Q S_{Ref} (SM)$$

$$\Delta m_t = \Delta N_t L_T$$

$$\Delta m_t = \left( \frac{C_N}{\delta} \right) (-\delta) Q S_{Ref} L_T$$

- Total moment about CG,

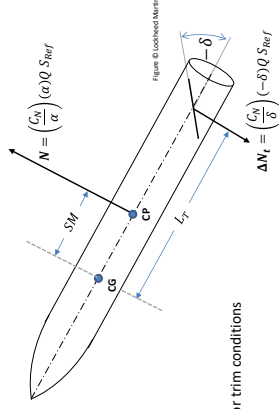
$$m_{CG} = m + \Delta m_t$$

- For trim,  $m_{CG} = 0$ ,

$$0 = m + \Delta m_t$$

- The fin deflection required for trim conditions

$$\delta = \frac{(C_N/\alpha) \alpha (SM)}{(C_N/\delta) L_T}$$



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## Rowan University Missile Design Variation

- As a result, there is tremendous variation in missile design

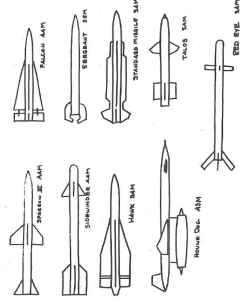


Illustration taken from Reference 1

The Missile Design Engineer's Optimum Design is Really the "Least Worst" Design

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- Refers to the condition at which the aerodynamic moments on the interceptor are balanced by the control surfaces
- The amount of tail deflection ( $\delta$ ) required to trim an interceptor is a function of  $SM$  and the tail control effectiveness,  $C_N/\delta$
- Tail deflection required for trim
  - $\delta = \frac{(C_N/\alpha) \alpha SM}{(C_N/\delta) L_T}$
  - Where:
    - $L_T$  is the distance from the CG to the tail control surface
- Since maximum tail deflection is fixed, a large static margin reduces the maximum trim angle of attack that can be achieved
- Large static margin is very stable, but provides a sluggish interceptor response

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## Rowan University Missile Body Design Trade Space

- The missile designer must
  - Consider the aerodynamic configuration and estimate basic aerodynamic parameters needed for performance and stability analysis
  - Determine the propulsion system requirements considering the mission requirements for range, speed, time-to-intercept and maneuverability
- The final missile design is a compromise of the requirements and preferred approaches of the following design disciplines
  - Aerodynamics
  - Propulsion
  - Structural design
  - Stability, Guidance and Control
  - Thermodynamics
  - Trajectory kinematics
  - Lethality (warhead – fuze)

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## Rowan University External Missile Body

- Illustration of the major missile body parts that affect missile aerodynamics

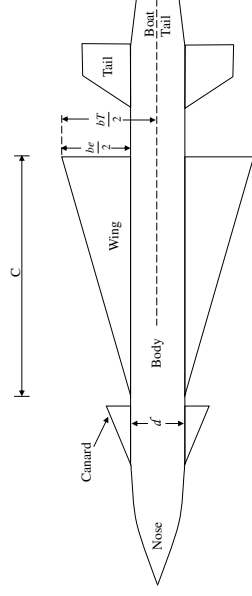


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- One of the most important design decisions is body diameter
- There are very few drivers for having a small missile body diameter
  - Decreases drag
  - Launch platform capability
- There are many drivers for having a large missile body diameter
  - Increases seeker performance
    - Higher resolution
    - Lower noise
  - Increases blast fragmentation and warhead effectiveness
    - Larger diameter → higher velocity fragments
  - Subsystem packaging (more room for your stuff)
  - Reduced CG travel and greater bending stiffness

The Desire for a Low Drag Airframe Results in a Small Missile Body Diameter Despite All the Reasons for a Large Body Diameter

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- Nose shape requirements are driven by the presence of a seeker
- Missiles without a seeker can use a pointed nose cone
- Missiles with a seeker require a trade-off between low drag and good radome characteristics for accurate sensor measurements

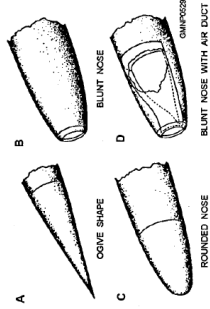


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- Airfoils are the wings, fins, etc. that are attached to the missile body
  - Provide flight stability
  - Provide lift
  - Control the missile's flight path (movable surface)
- The traditional missile body has 3 potential control surfaces
  - Canard
  - Wing
  - Tail
- Taking advantage of the unique control surfaces of a missile allows one to
  - Create a robust guidance law
  - Design for optimal conditions
  - Improve performance

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- Body fineness ratio (BFR) is the ratio of the missile length to the missile diameter
 
$$BFR = \frac{\text{length}}{\text{diameter}}$$
- Typical range of the BFR is 5 to 25
  - Portable anti-air missile have low BFR (Javelin)
  - Air-to-air missiles have high BFR (AMRAAM)
- Benefits of a large body diameter
  - Improved seeker and warhead effectiveness
  - Reduced CG movement during rocket motor burn
  - Greater bending stiffness
  - More internal volume
  - Reduced pitching and yawing inertia
- Benefits of a small body diameter
  - Missile drag

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- Nose fineness ratio (NFR) is the ratio of the nose length to the max. nose diameter
 
$$NFR = \frac{\text{length}}{\text{diameter}}$$
- Benefits of a high NFR (~5)
  - Excellent aerodynamics
  - Low observables
  - Reduces wave drag
- Benefits of a low NFR (~0.5)
  - Minimal radome slope errors
- Typical range of the NFR is 2 to 4 for supersonic missiles

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View from Side

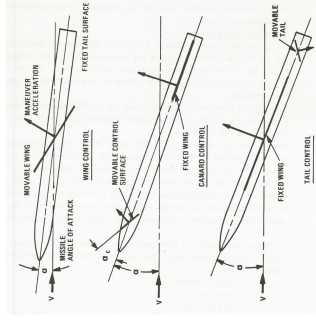


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View from Aft

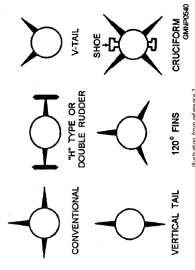


Illustration from reference 2

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| Control Type | Characteristics                                                                                                                | Pro                                                                                                                                                                                                        | Con                                                                                                                                                                              |
|--------------|--------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Wing         | <ul style="list-style-type: none"> <li>Low angle of attack during the maneuver</li> </ul>                                      | <ul style="list-style-type: none"> <li>Desirable for air breathing engines (because high <math>\alpha</math> may cause the engine to stall)</li> </ul>                                                     | <ul style="list-style-type: none"> <li>Significant structural weight</li> <li>Large actuation system needed to move the wing</li> </ul>                                          |
| Canard       | <ul style="list-style-type: none"> <li>Lower <math>\alpha</math> than tail, higher than wing</li> </ul>                        | <ul style="list-style-type: none"> <li>Limited to max <math>\alpha = 45^\circ</math></li> <li>Physical location is where guidance equipment is normally located</li> </ul>                                 | <ul style="list-style-type: none"> <li>Limited a capability due to control surface saturation</li> <li><math>\alpha_{canard} = \delta_{canard} + \alpha_{body}</math></li> </ul> |
| Tail         | <ul style="list-style-type: none"> <li>Vector force produced by control surface is opposite of the desired maneuver</li> </ul> | <ul style="list-style-type: none"> <li>High <math>\alpha</math> capability</li> <li><math>\alpha_{tail} = \delta_{tail} - \alpha_{body}</math></li> <li>Good physical location (no competition)</li> </ul> | <ul style="list-style-type: none"> <li>Lift produced by wing and body must overcome tail force to achieve desired acceleration</li> </ul>                                        |

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- Non-traditional means of controlling the missile flight are also common
- Thrust controllers
  - Thrust Vector Actuator (TVA)
    - Nozzles typically located at the rear of the missile which generate a directional thrust for the purpose of changing missile flight path
  - May be the main rocket motor or an auxiliary thrust for the flight path control only
  - Thrust Vector Controller (TVC)
    - Vane inserted into (or just outside) of the rocket motor nozzle to deflect thrust
- Attitude control motors
  - Small explosives in the missile which are fired to generate a nearly instant change angle of attack, thus inducing an normal force

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- Benefits of small or no wings
  - Increased range in high supersonic flight / high dynamic pressure
  - Provides better stability and control at high angles of attack
  - Lower radar cross section (RCS)
  - Launch platform compatibility (packaging, storage)
- Benefits of larger wings
  - Increased range in subsonic flight / low dynamic pressure
  - Lower guidance time constant (more maneuverable)
  - More capability at higher altitudes
  - Less seeker error due to dome error slope (lower angle of attack)
  - Lower gimbal requirements for seeker

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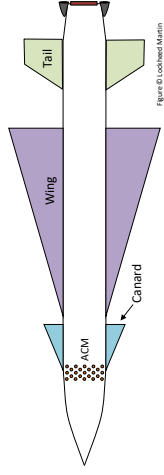
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- Lift effectiveness ( $C_{L\alpha}/\alpha$ ) is a must
  - High wing/lift with a low angle of attack
  - High missile response to commands
  - Low drag penalty
- Well thought out control surface positioning
  - Designed for good control and stability
  - Must provide minimum torque due to airloads (location of hinge line)
- Minimum interference of wings with armament effectiveness
  - Wings are often set aft of the warhead

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- A missile's flight is controlled through the deflection of various missile surfaces
  - Tail
  - Wing
  - Canard
- Additional means of controlling flight are also possible
  - Thrust Vector Actuator – Jets located near the tail of the missile (TVA) ➔
  - Thrust Vector Control – Surface which deflects the thrust of the rocket motor (TVC) ➔
  - Attitude control motors (ACM) ➔



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1. Missile System Engineering Fundamentals. *Missile Aerodynamics*, Lockheed Martin Course, ~1984
2. NAVEDTRA 14110, *Gunner's Mate 1 & C*. November 1996
3. Fleeman, Eugene. *Missile Design Guide*. American Institute of Aeronautics and Astronautics, Inc. 2022

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