

Homework 5 - Aidan Sharpe

1

If the specific weight, γ , of a substance is $8.2[\text{kN}/\text{m}^3]$, what is its mass density, ρ , in kg/m^3 ?

On Earth, $9810[\text{kg}]$ weighs $1[\text{kN}]$, so an object that weighs $8.2[\text{kN}]$ will have a mass of $80442[\text{kg}]$. Therefore, $\rho = 80442[\text{kg}/\text{m}^3]$.

2

A fluid flowing between two parallel plates has a viscosity, $\mu = 0.62[\text{Ns}/\text{m}^2]$, and density, $\rho = 1250[\text{kg}/\text{m}^3]$. Calculate the intensity of shear stress, τ , in pascals at $y = 3[\text{cm}]$, assuming a straight-line viscosity distribution, given that the top plate has a velocity of $100[\text{cm}/\text{s}]$ and the fluid is $6[\text{cm}]$ thick.

Velocity at $y = 3[\text{cm}]$:

$$\tau = \mu \frac{du}{dy} = 0.62 \left(0.03 \times \frac{1}{0.06} \right) = 0.31[\text{Pa}]$$

3

A cube with side length $10[\text{cm}]$ is placed into two different liquids. In the first liquid, the top of the cube is $h_1 = 1[\text{cm}]$ above the surface. In the second liquid, the top of the cube is h_2 above the surface. If the densities of the liquids are known to be $\rho_1 = 1000[\text{kg}/\text{m}^3]$, and $\rho_2 = 1300[\text{kg}/\text{m}^3]$ respectively, find h_2 .

Displaced mass for liquid 1, same as mass of cube:

$$0.1 \times 0.1 \times (0.1 - 0.01) \times 1000 = 0.9[\text{kg}]$$

Displaced mass for liquid 2:

$$0.1 \times 0.1 \times (0.1 - h_2) \times 1300 = 0.9$$

$$\therefore h_2 = 0.031[\text{m}] = 3.1[\text{cm}]$$